## Math 10460 - Honors Mathematics II Homework 12c - Due Wednesday, April 20

You must show your work in all of the problems!!!

Recall that  $S^2$  is the sphere,  $\mathbb{T}$  is the torus, and  $\mathbb{K}$  is the Klein bottle.

(7) If k, n > 0, then

$$k\mathbb{P} \# n\mathbb{T} = m\mathbb{P}$$

for some m. Find m in terms of k and n. Recall that  $\mathbb{P}\#\mathbb{T}=3\mathbb{P}$ .

(8) Suppose the surface  $\Sigma$  can be represented as a polygon with word given by

$$ab^{-1}a^{-1}cb^{-1}c$$

Use the classification theorem to write  $\Sigma$  as  $S^2$ ,  $g\mathbb{T}$ , or  $m\mathbb{P}$ .